

# AGENT-ORIENTED PROGRAMMING: FROM THEORY TO PRACTICE

Costin Bădică

*University of Craiova  
Department of Computers and Information Technology*

# UNIVERSITY OF CRAIOVA



# IDS RESEARCH GROUP

- *Intelligent Distributed Systems Research Group*
- <http://ids.software.ucv.ro/>
- Synergies between:
  - Intelligent computing
  - Distributed computing



# OVERVIEW

## I. Basics of AOP

*BDI*

*Logic-based*

## II. Examples

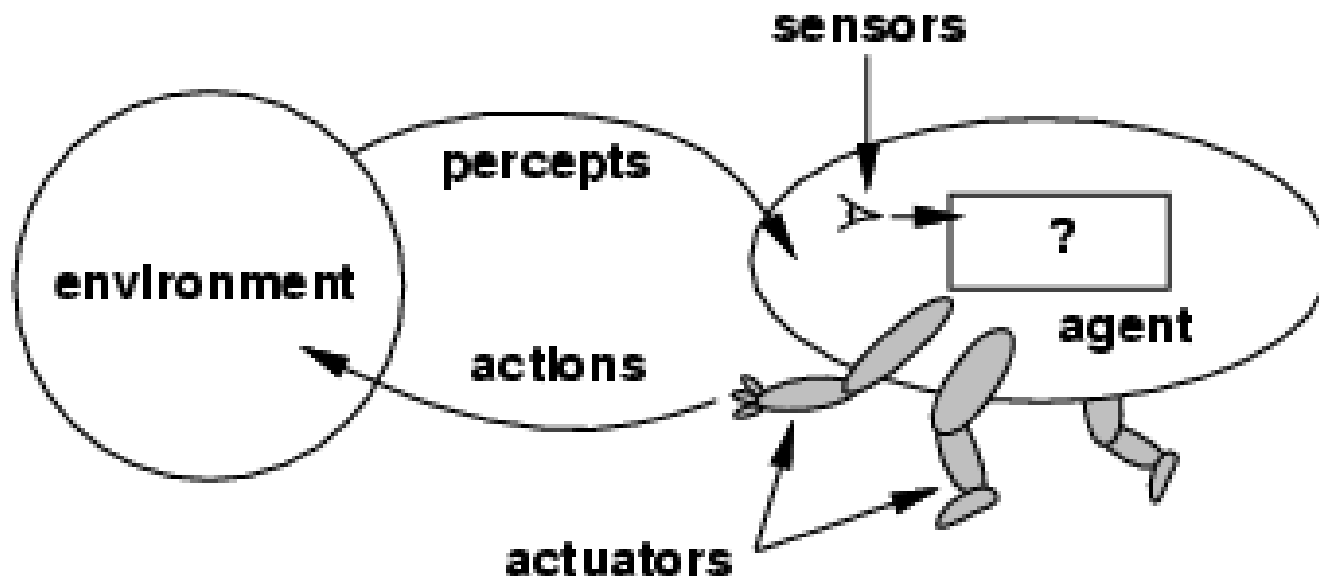
*Modeling and Enactment of Business Agents*  
*Programming Reinforcement Learning*  
*Freight Transportation Exchanges*

# ORIGIN OF WORD “AGENT”

- The word “Agent” comes from the Latin word “Agere”.
- It literally means “to do” with the sense of “to act” or “to take action”.

# AGENTS AND ENVIRONMENTS

- (Weakest) Agent = anything that can be viewed as:
  - *perceiving* its environment through *sensors* and
  - *acting* upon that environment through *actuators*.
 [Russel & Norvig, 2010]



# ENVIRONMENTS

- (Fully / Partially / Not) Observable:
  - Noisy & inaccurate sensors
  - Immeasurable / inaccessible parts of the environment
- (Single / Multi) Agent
  - *Competitive*: multiple agents with disjoint goals
  - *Cooperative*: multiple agents sharing (parts of) goals
- Deterministic / Stochastic
  - *Deterministic*: environment state completely determined by agent action
  - *Nondeterministic*: probabilities of next states are missing
  - *Uncertain*: partially observable and stochastic

# MAS TECHNOLOGIES

- Methodologies
- Standards
- Frameworks and platforms
- *Programming languages*
- Other technologies



# AGENT ORIENTED PROGRAMMING

- AOP was firstly proposed 25 years ago as:

*A new programming paradigm, one based on cognitive and societal view of computation  
[Shoham, 1993]*

- Many models and implementations of AOP ! One representative class is based on:

*Belief-Desire-Intention architecture – BDI.*

# AGENTSPEAK(L) AND JASON

- AgentSpeak(L) = *abstract AOP language* (Rao, 1996)
- Jason = implementation and extension of AgentSpeak(L), based on Java.
  - *Agent program* is written in Jason.
  - *Environment* is written in Java.
  - *Agent architecture* can be customized in Java.
- AgentSpeak(L) combines *BDI* and *Logic*

# SOURCE OF INSPIRATION

- Philosophy: Daniel Dennett’s “intentional stance”:
  - Distinguish between mental and physical phenomena by means of “intentionality”.
  - Explain behavior of an (artificial) entity in terms of its “mental properties”.
- Dennett introduced BDI concepts:
  - belief, desire, goal, practical reasoning, ...

# BDI CONCEPTS

- BDI follows practical reasoning model = *reasoning towards actions*.
- BDI agents are endowed with:
  - *Beliefs*
  - *Desires* or *goals*
  - *Intentions* or *plans*
- Agent behavior is *event-driven*.

# AGENT PROGRAM

- Initial belief base: *set of facts and rules*:  
 $predicate(term_1, \dots, term_n)$
- Initial goal(s): *achievement goals*  
 $!predicate(term_1, \dots, term_n)$
- Plan base: *set of plans*:  
 $event : context \leftarrow plan\ body$
- Event:  $+ !goal \quad - !goal \quad +belief \quad -belief$
- Context: Conjunctive (&) / disjunctive (|) *condition*
- Plan body: *sequence of actions* separated by ;

# BDI REASONING STEPS

- Update

perceive  
communicate

- Select

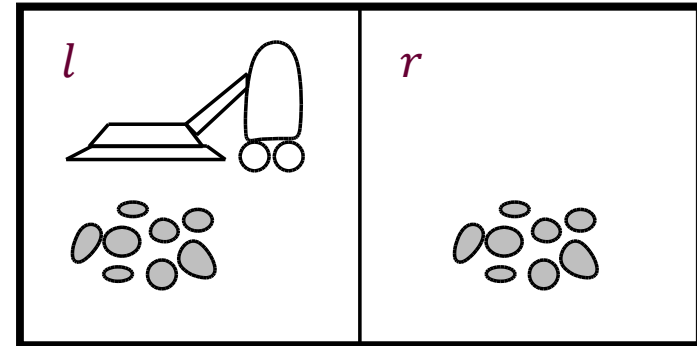
event  
applicable plan  
intention = course of action

- Act

internal / external  
mental note  
adopt / drop goal:  
test / achievement

Deliberation cycle

# VACUUM CLEANER WORLD



- Environment:
  - 2 locations  $l$  and  $r$
  - Status of the current location: *clean* or *dirty*.
- Actions:
  - *left*, *right*, *suck*, *no\_op*, for “move left”, “move right”, “suck dirt” and “do nothing”.
- Percepts:
  - Pair  $[pos(Location), Status]$ , for example  $[pos(l), dirty]$

# REACTIVE / PROACTIVE

```
+pos(l) : clean <-
  .print("l clean");
  right.
+pos(l) : dirty <-
  .print("l dirty");
  suck;
  right.
+pos(r) : clean <-
  .print("r clean");
  left.
+pos(r) : dirty <-
  .print("r dirty");
  suck;
  left.
```

```
!keep_clean.
+!keep_clean : dirty &
  pos(L) <-
  .print("suck in ",L);
  suck;
  !move.
+!keep_clean : clean &
  pos(L) <-
  .print("no suck in ",L);
  !move.
+!move : pos(l) <-
  right;
  !keep_clean.
+!move : pos(r) <-
  left;
  !keep_clean.
```



# LOGIC PROGRAMMING

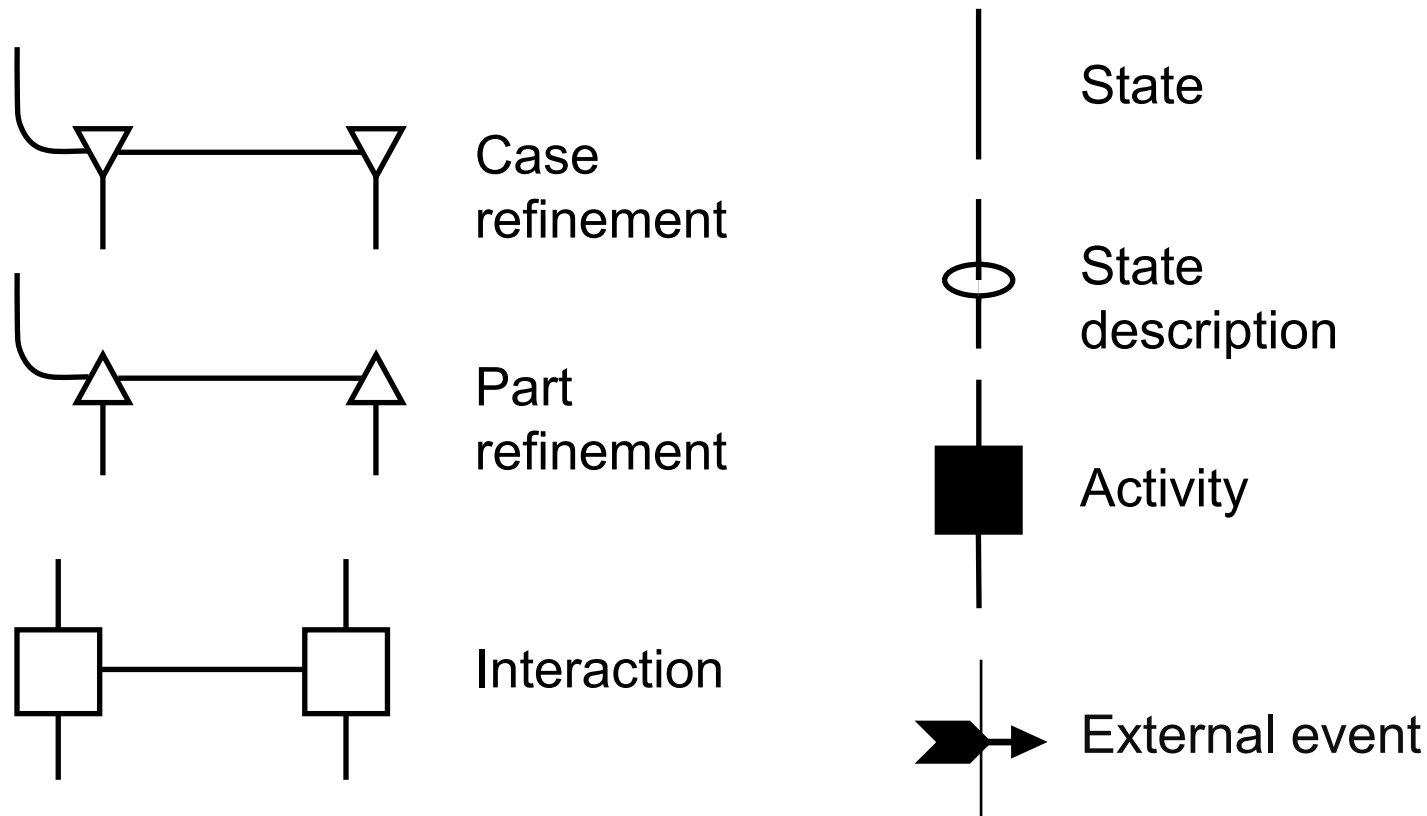
Logic Program = Facts + Rules + Queries

  
Belief Base

  
Test goals

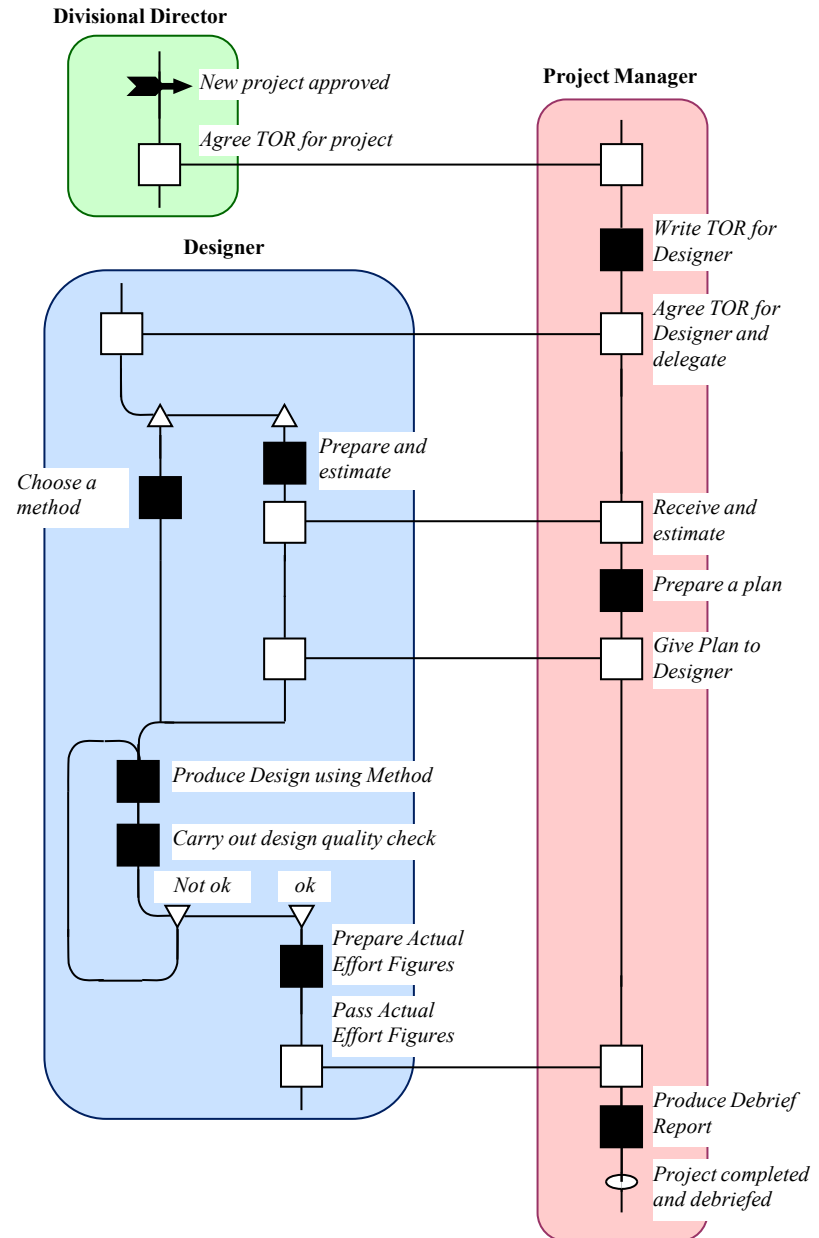
# BUSINESS AGENTS

- **AIM:** *apply state-of-the-art AOP languages for modeling and enactment of business processes.*



# ROLE ACTIVITY DIAGRAM

- Three roles:
  - Divisional Director
  - Project Manager
  - Designer



# MAPPING OUTLINE

- **RAD role** => Jason agent. Eg.: *d*, *dd*, *pm* agents.
- **State** => belief base. E.g.: *dd0*, *dd1*, *dd2*, *d0*, *d1*, ...
- **Action** => agent plan:

**+!advance** : *current state* <-

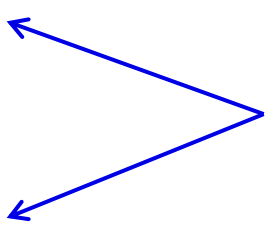
*remove tokens*

*do activity*

*append tokens*

**!advance.**

*state update*



- **RAD process** => multi-agent program

# MAPPING STATES AND ACTIVITIES

```

+!advance : dd0 <-
  -dd0;
  ?task("New project approved");
  +dd1;
  !advance.
    
```

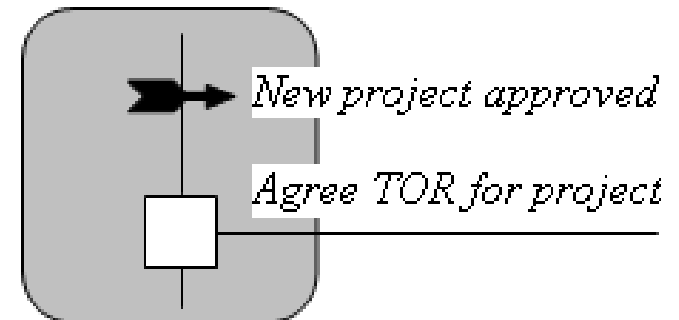
```

+!advance : start <-
  -start;
  ?task("Starting ...");
  +dd0;
  !advance.
    
```

```

+!advance : dd2 <-
  -dd2;
  ?task("Stop").
    
```

**Divisional Director**



Start state

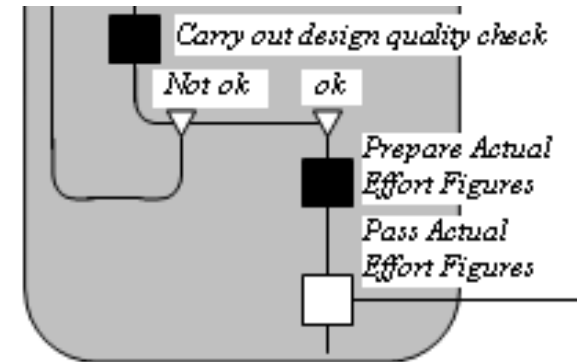
End state

# MAPPING CASE REFINEMENTS

```

+!advance : d9 <-
  -d9;
  ?task("Carry out design quality check");
  rad.choice([ok,nok],Result)
+d10(Result);
!advance.

+!advance : d10(nok) <-
  -d10(nok);
  ?task("Design quality not ok");
+d8;
!advance.
    
```



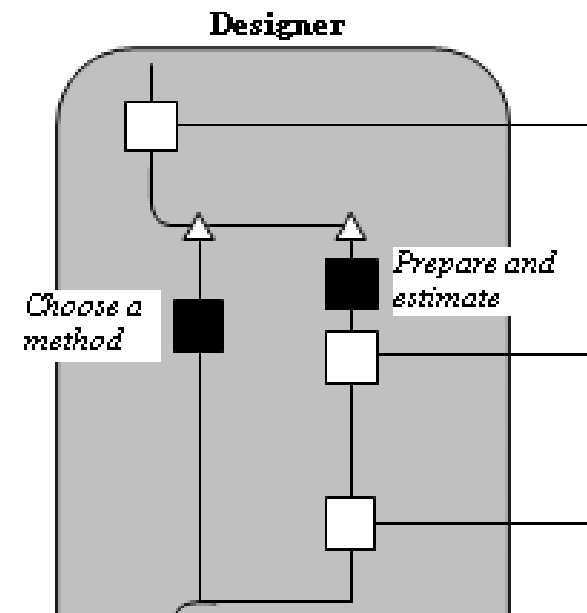
# MAPPING PART REFINEMENTS

```

+!advance : d1 <-
  -d1;
  ?task("Fork parallel threads");
  +d2;
  +d3;
  !advance.
    
```

```

+!advance : d6 & d7 <-
  -d6;
  -d7;
  ?task("Join parallel threads");
  +d8;
  !advance.
    
```

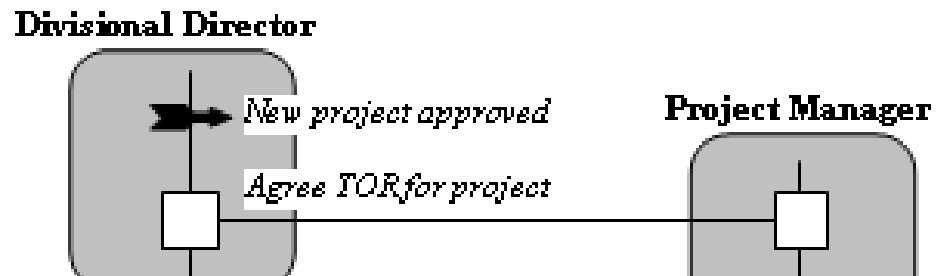


# MAPPING INTERACTIONS

```

+!advance : start <-
  -start;
  ?task("Starting ...");
  +pm0;
  .send(dd,tell,pm0);
  !advance.

+!advance : dd1 & pm0 <-
  -dd1;
  -pm0 [source (pm)];
  ?task("Agree TOR for project");
  +dd2;
  !advance.
    
```





# CONTINGENCY PLAN

```

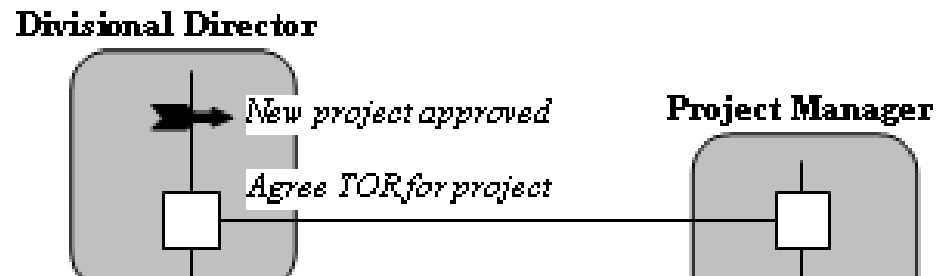
+!advance : dd1 & pm0 <-
  -dd1 ;
  -pm0 [source (pm) ] ;
  ?task("Agree TOR for project") ;
  +dd2 ;
  !advance .
    
```

```

-!advance : true .
    
```

```

+pm0 : true <- !advance .
    
```



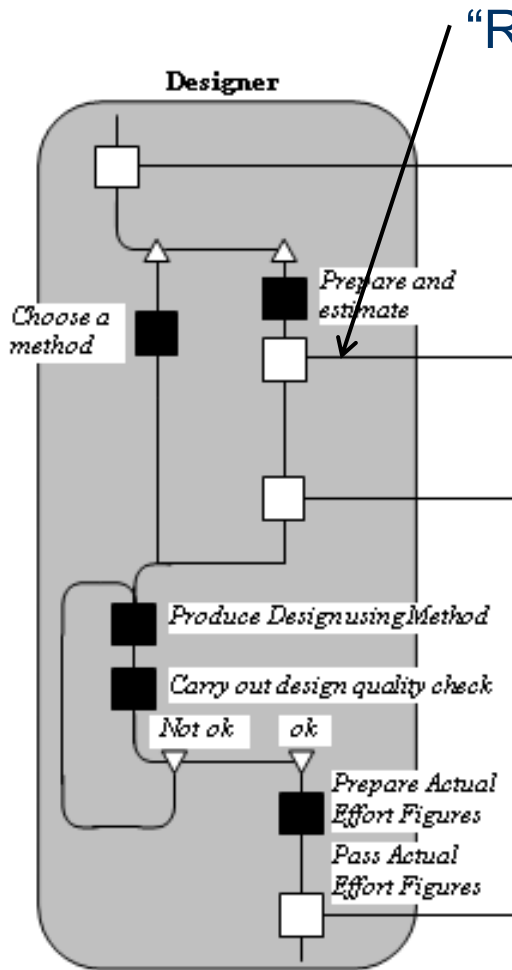
# MAPPING SUMMARY

- *One proactive plan* for agent starting and one proactive plan for agent stopping.
- *A proactive plan* for each action node.
- *One contingency plan* to deal with shared beliefs that have not yet arrived from peer agents.
- *A reactive plan* for handling the arrival of each shared belief from peer agents.

# KNOWLEDGE-BASED BUSINESS AGENTS

- Generic *knowledge-based business agent architecture* –  $\mathcal{KB}^2\mathcal{A}^2$ .
  - A *knowledge base* that captures the operational knowledge of the agent according to a given business process.
  - A *set of template plans* that capture the generic behavioral patterns of business agents.

# KNOWLEDGE BASE



“Receive and estimate”

```
% rule (Action, StateIn, StateOut) .
```

```
rule(task("Fork parallel threads"), [d1], [d2, d3]) .
```

```
rule(task("Prepare and estimate"), [d3], [d4, s(pm, d4)]) .
```

```
rule(task("Receive and estimate"), [d4, r(pm, pm3)], [d5, s(pm, d5)]) .
```

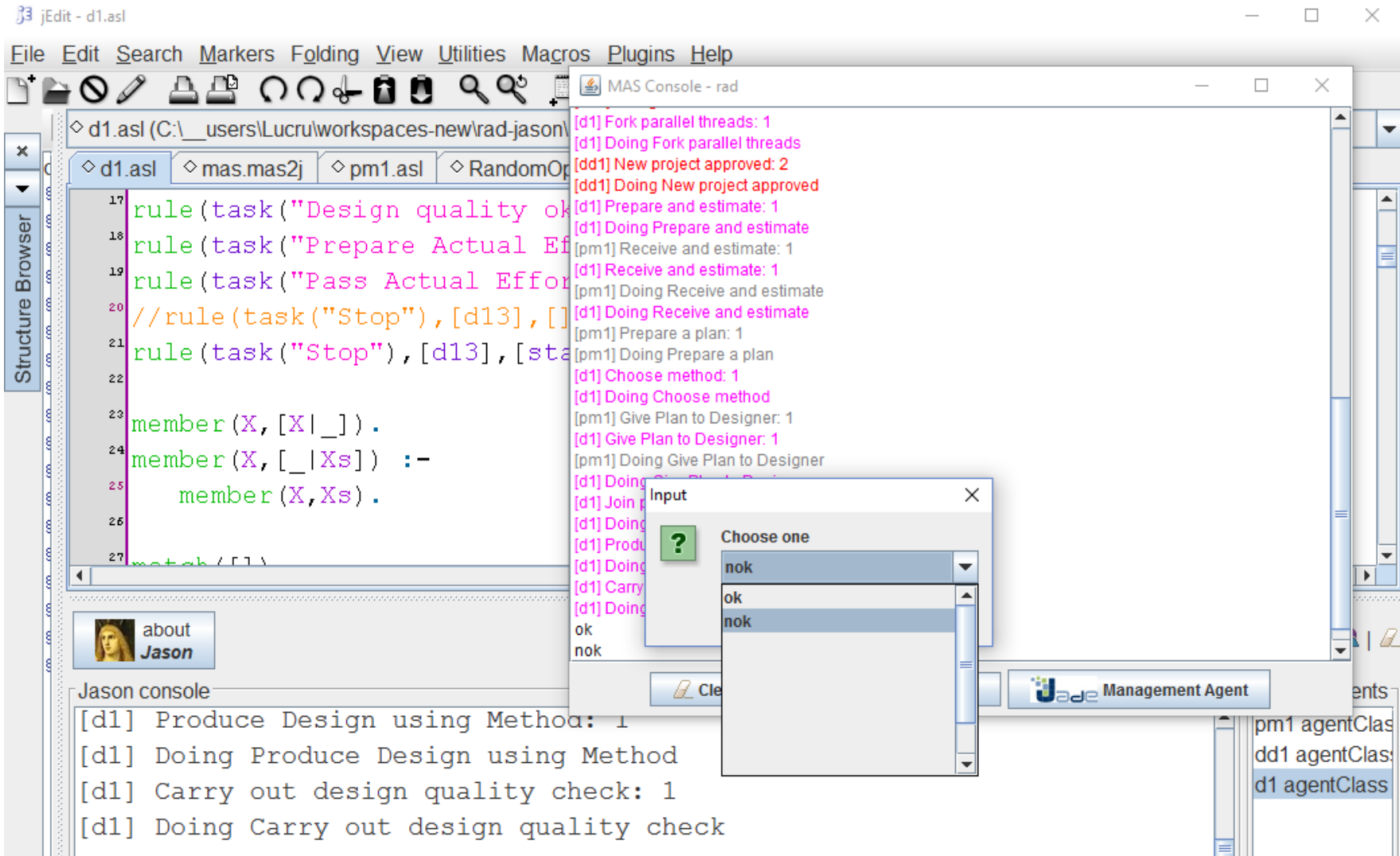
...

```
rule(choice("Carry out design quality check", [ok, nok]), [d9], [[ok, d10(ok)], [nok, d10(nok)]]).
```

Send shared belief

Receive shared belief

# *KB<sup>2</sup>A<sup>2</sup>* IN ACTION



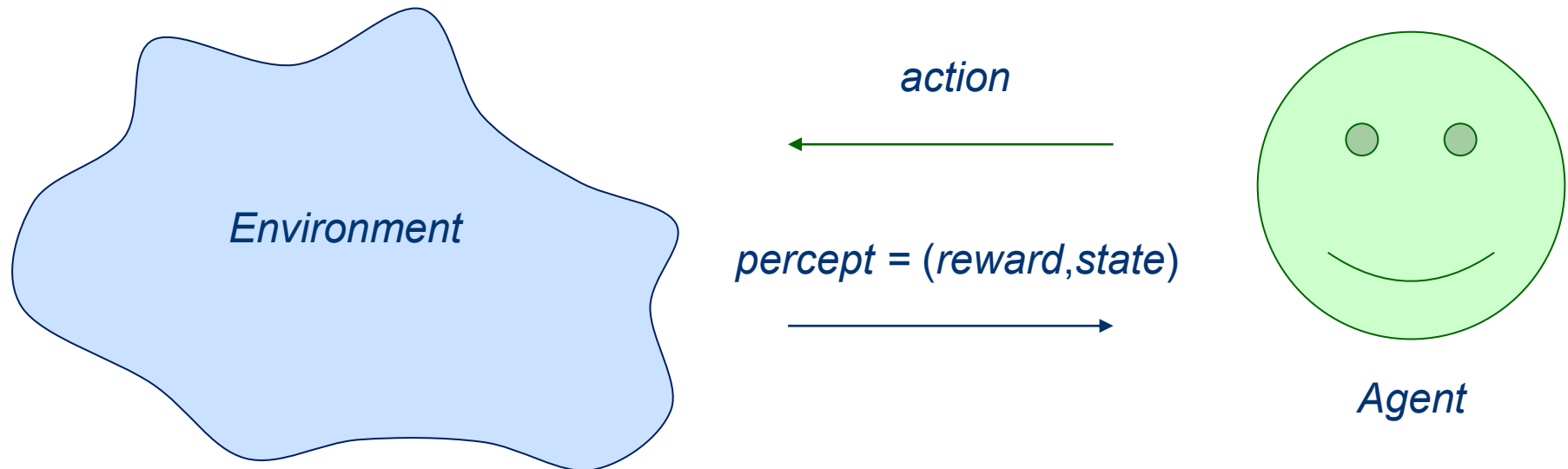
The screenshot displays the jEdit IDE with the file `d1.asl` open. The code in the editor includes rules for tasks like "Design quality check", "Prepare Actual Effort", and "Pass Actual Effort", along with member declarations for `X`. The MAS Console window shows a sequence of execution messages, including:

- [d1] Fork parallel threads: 1
- [d1] Doing Fork parallel threads
- [dd1] New project approved: 2
- [dd1] Doing New project approved
- [d1] Prepare and estimate: 1
- [d1] Doing Prepare and estimate
- [pm1] Receive and estimate: 1
- [d1] Receive and estimate: 1
- [pm1] Doing Receive and estimate
- [d1] Doing Receive and estimate
- [pm1] Prepare a plan: 1
- [pm1] Doing Prepare a plan
- [d1] Choose method: 1
- [d1] Doing Choose method
- [pm1] Give Plan to Designer: 1
- [d1] Give Plan to Designer: 1
- [pm1] Doing Give Plan to Designer
- [d1] Doing Give Plan to Designer
- [d1] Join
- [d1] Doing
- [d1] Produ
- [d1] Doing
- [d1] Carry
- [d1] Doing
- ok
- nok

An "Input" dialog box is open, prompting "Choose one" with a list containing "nok", "ok", and "nok". The Jason console at the bottom shows the following messages:

```
[d1] Produce Design using Method: 1
[d1] Doing Produce Design using Method
[d1] Carry out design quality check: 1
[d1] Doing Carry out design quality check
```

# PROGRAMMING REINFORCEMENT LEARNING



- Passive RL: agents act according to a fixed policy and their learning goal is to compute the utility function.
- Active RL: agents learn an optimal policy that maximizes their utility, while they are acting in their environment.

# REINFORCEMENT LEARNING

- Markovian stochastic environment  $E$ .
- For each state  $e$  agent receives *reward*  $R(e)$
- Agent behavior defined by *policy*  $\pi: E \rightarrow A$ .  
 $a = \pi(e)$  is agent *action* in environment state  $e$ .
- Agent starting in state  $e$  generates a *history*:

$$H(e) = [e_0 = e, e_1, \dots, ]$$

- Each history awards agent with *utility*:

$$U_h(H(e)) = \sum_{i \geq 0} \gamma^i R(e_i)$$

- *Utility of policy*  $\pi$  is:

$$U^\pi(e) = \mathbb{E}[U_h(H(e))]$$

# PASSIVE REINFORCEMENT LEARNING

- **Goal**: For given policy  $\pi$  the agent learns  $U^\pi$ .
- **Temporal Difference Learning**:  
 for each observed state transition  $e \rightarrow e'$   
 the agent computes an updated  $U^\pi(e)$  as follows:

$$U^\pi(e) + \alpha(R(e) + \gamma U^\pi(e') - U^\pi(e))$$



# ACTIVE REINFORCEMENT LEARNING

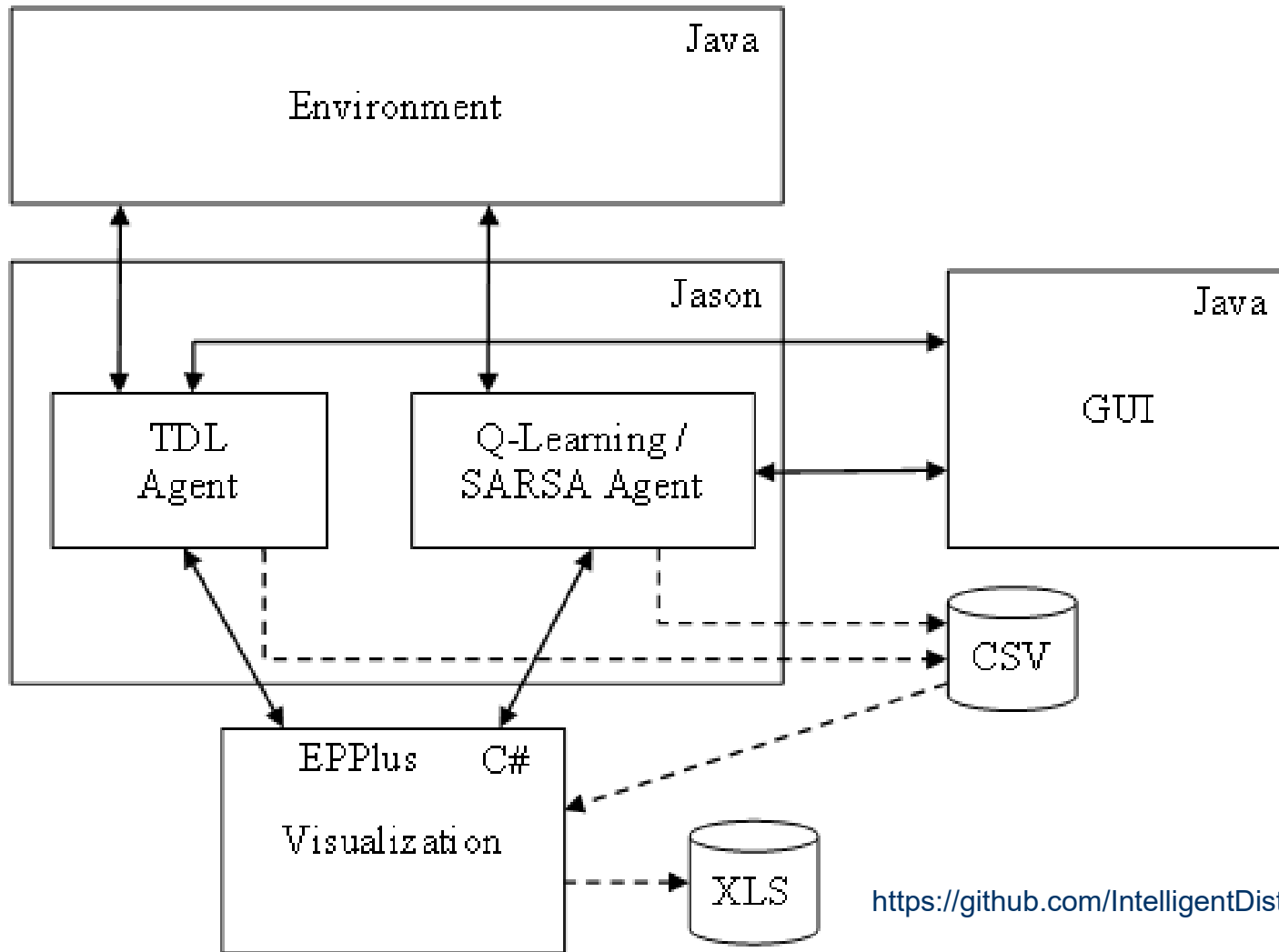
- **Goal:** Compute the optimal policy  $\pi^*$  that maximizes  $U^\pi$ . Let  $U(e) = U^{\pi^*}(e)$ .
- $Q(e, a)$  = utility of taking action  $a$  in state  $e$  so  

$$U(e) = \max_{a \in Ac} Q(e, a)$$
- **Q-learning:** update  $Q(e, a)$  for each transition  $e \rightarrow e'$   

$$Q(e, a) + \alpha(R(e) + \gamma \max_{a' \in Ac} Q(e', a') - Q(e, a))$$
- **SARSA:**  $a'$  is the actual action taken in state  $e'$   

$$Q(e, a) + \alpha(R(e) + \gamma Q(e', a') - Q(e, a))$$

# SYSTEM ARCHITECTURE

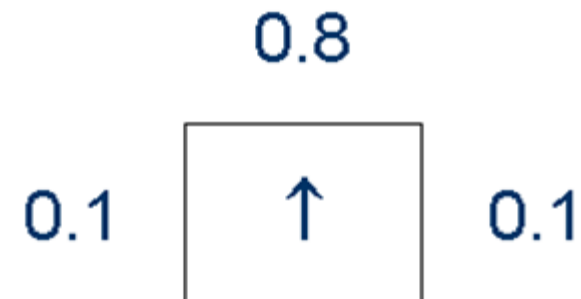


<https://github.com/IntelligentDistributedSystems/SamuelFelton>

# ENVIRONMENT

- Class *MDPModel* to store & update environment state
- Class *MDPEnv* to interface with Jason interpreter
- Class *MDPView* – GUI & visualization

3	→	→	→	+1
2	↑		↑	-1
1	↑	←	←	←
	1	2	3	4



# ACTIONS & PERCEPTS

- Agent actions:
  - *up*, *right*, *down*, *left* for the agent movement
  - *null*, for restarting a new trial in a random initial position.
  
- Agent percepts  $pos(Row, Column, R, T)$  such that:
  - *Row* and *Column* give the agent position on the grid
  - *R* is the reward.
  - *T* is *n* for non-terminal state and *t* for terminal state

# ENVIRONMENT GUI

MDP View
— □ ×

**Environment**

Empty environment Ctrl-N  
 Size Ctrl-Z  
 Save Ctrl-S  
 Load Ctrl-O

	→ R: -0.04 U: 0.0 T: 0	→ R: -0.04 U: 0.0 T: 0	↓ R: -0.04 U: 0.0 T: 0	→ R: -0.04 U: 0.0 T: 0	↓ R: -0.04 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	
	↓ R: -0.04 U: 0.0 T: 0		R: -0.04 U: 0.0 T: 0	R: -1.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	
	R: -0.04 U: 0.0 T: 0	R: -0.04 U: 0.0 T: 0	R: -0.04 U: 0.0 T: 0	R: 1.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	
	R: 0.0 U: 0.0 T: 0		R: 0.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	
	R: 0.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0	R: 0.0 U: 0.0 T: 0			R: 0.0 U: 0.0 T: 0	

Free space

UP

-0.04

Validate

Run

# STATE SUMMARY

Stats: pos(1,3,n)

Action	Q-Value	Number of trials
DOWN	-0.2534336287468129	50
RIGHT	-0.27342072330776646	21
UP	-0.256	6
LEFT	0.7198818753530539	315
NULL	0.0	0

# AGENT CODE

- **Belief Base:**
  - Counters of states and trials
  - Maximum number of trials
  - Last and next action
  - Discount factor
  - Minimum number of state visits to encourage exploration
  - Utility and number of visits for each state
- **Goals**
  - Achievement goal: learning to act, i.e. determine Q-values
  - Acting = sequence of trials
  - Trial = sequence of moves
  - Update Q-values following each move

# Q-LEARNING AGENT

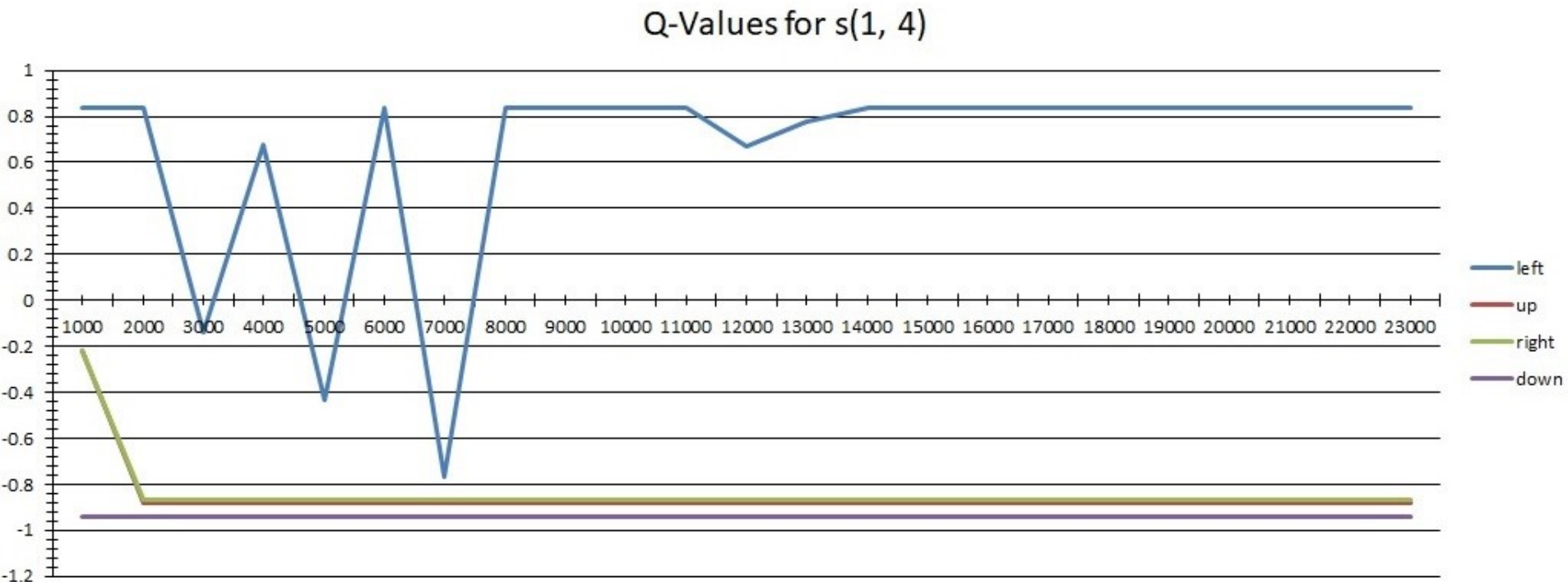
```

+!update_qvalue (St1,_,St,R,Q_St,A,M1) :
    non_terminal_state (St) <-
        .findall (Q,qvalue (St1,A1,Q,_),Qs) ;
    ?maxim_list (Qs,Q_St1) ;
    ?gamma (Discount) ;
    ?alpha (Alpha) ;
    Q1 = Q_St + Alpha* (R+Discount*Q_St1-Q_St) ;
    -qvalue (St,A,_,_) ;
    +qvalue (St,A,Q1,M1) .

+!update_qvalue (_,R1,St,_,_,null,M1) :
    terminal_state (St) <-
    -qvalue (St,null,_,_) ;
    +qvalue (St,null,R1,M1) .
    
```

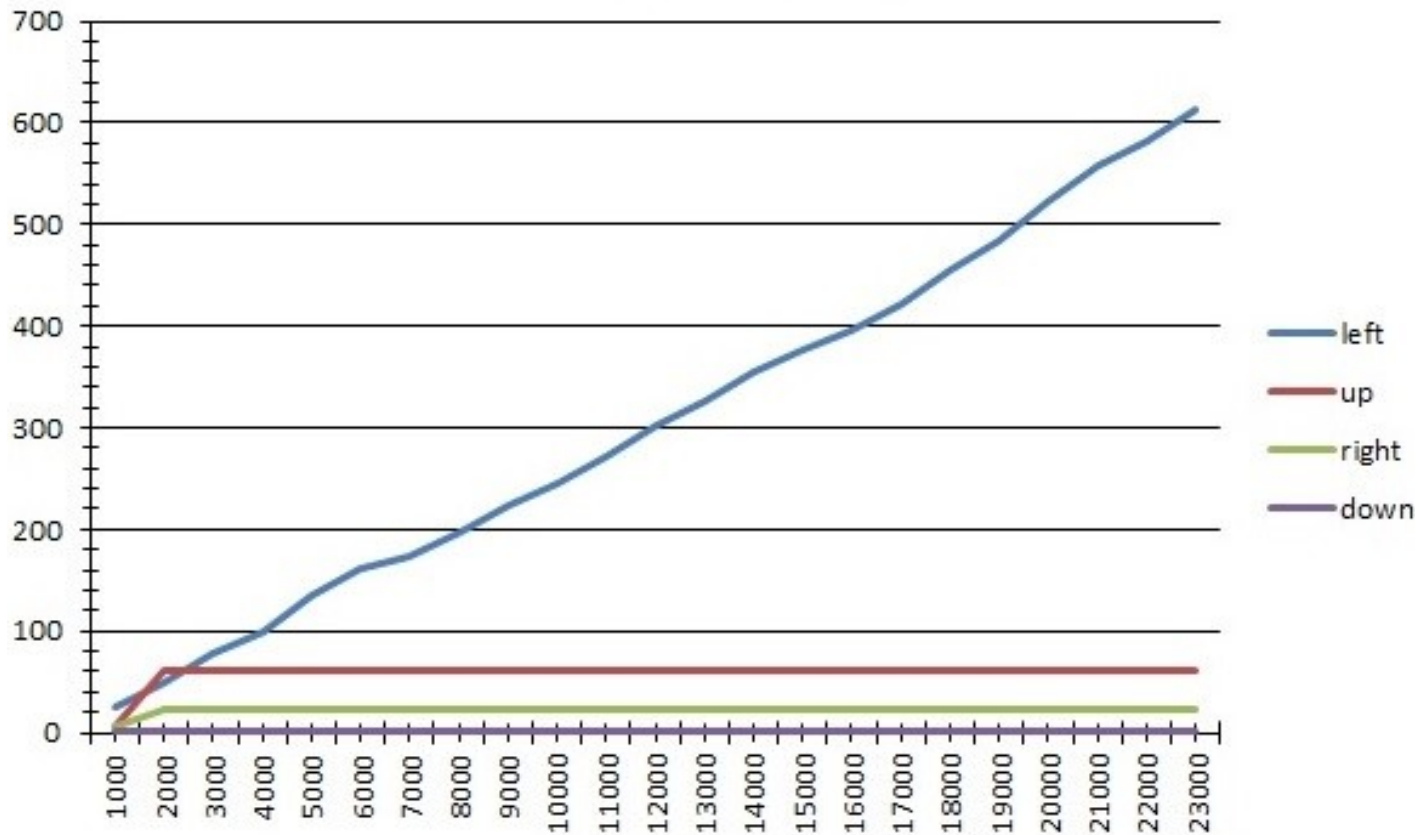


# Examining Q-values



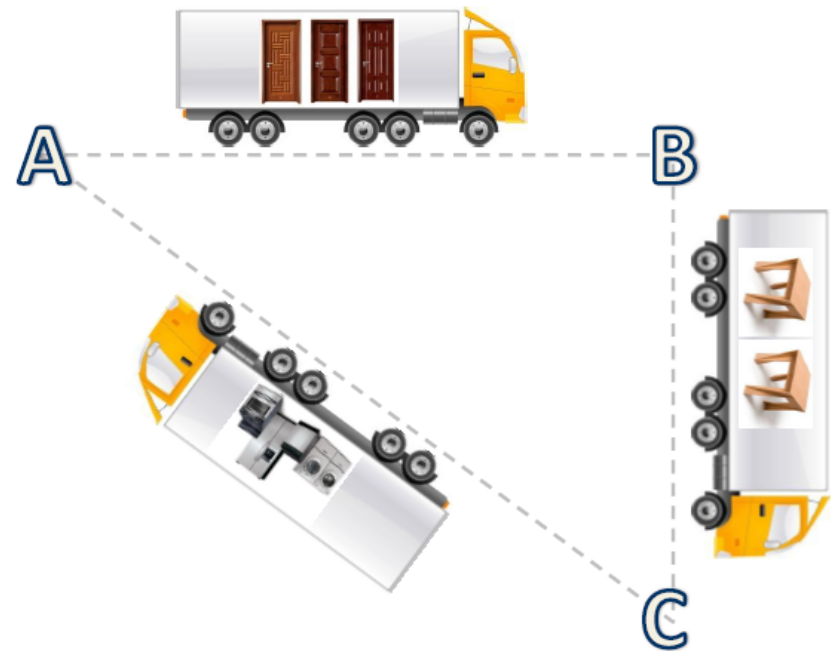
# NUMBER OF TRIALS

Trials for  $s(1, 4)$

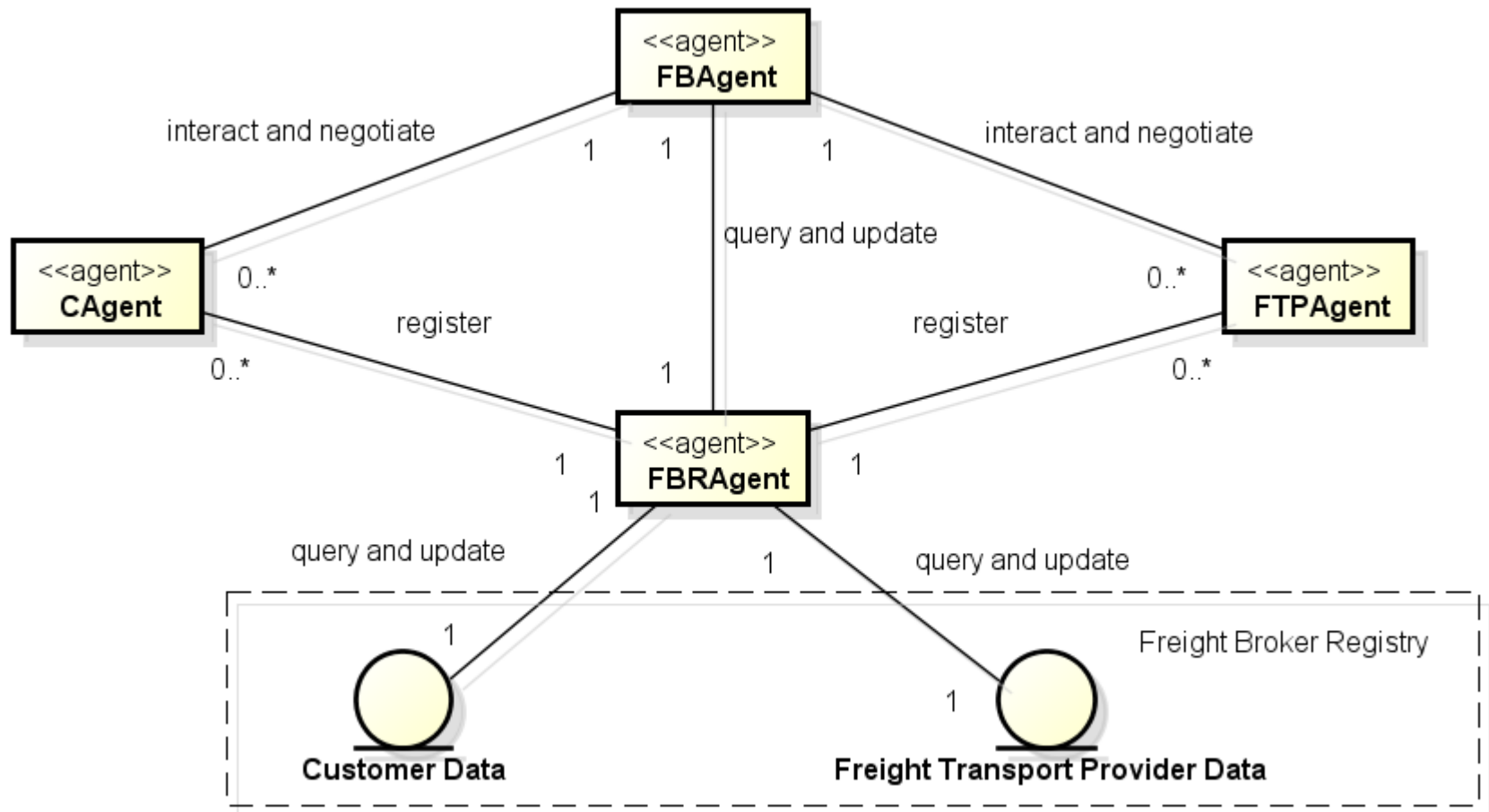


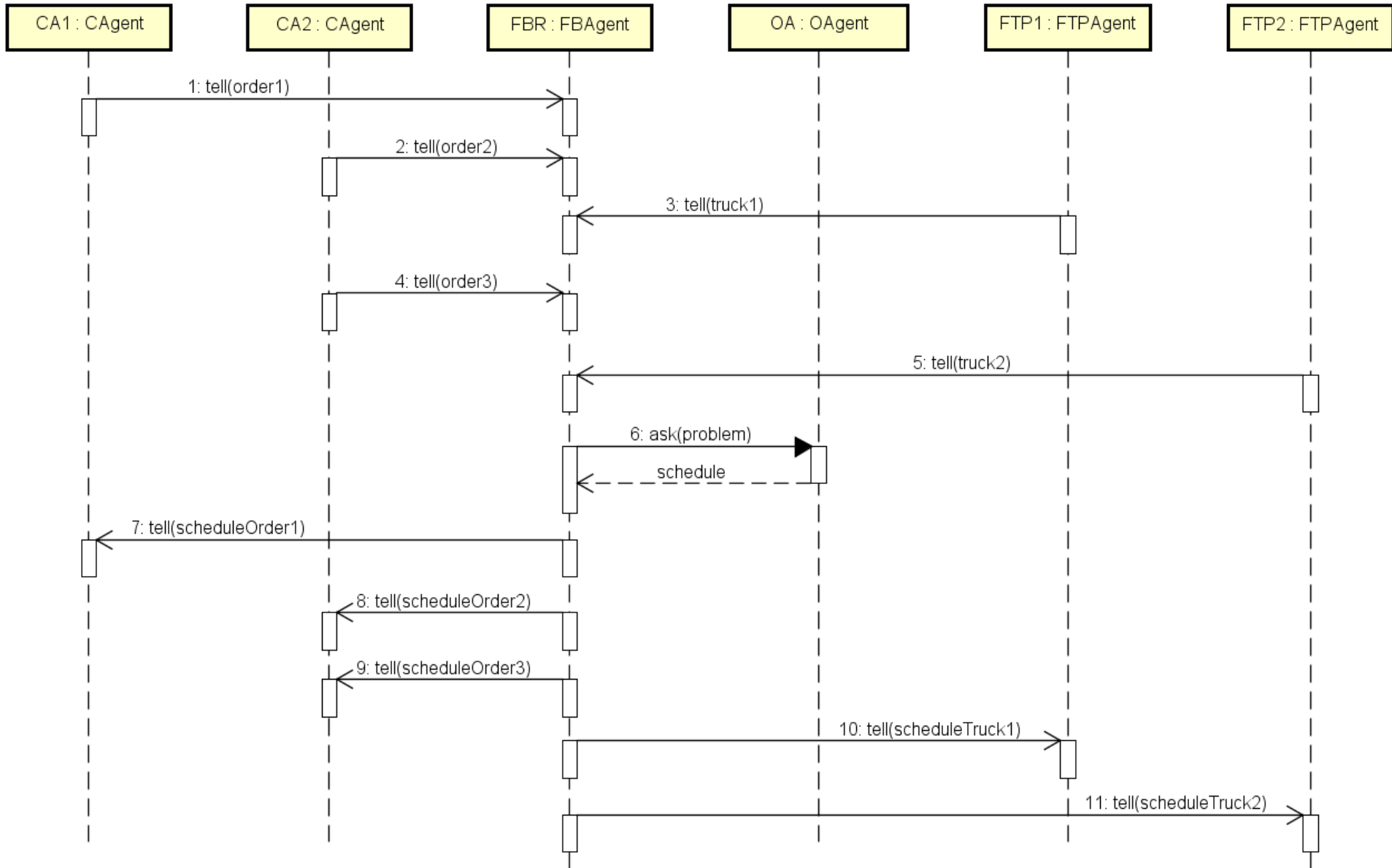
# FREIGHT TRANSPORTATION EXCHANGES

- Opportunity:
  - need of transporting goods
  - availability of free vehicles
- Goal:
  - capturing transportation opportunities
  - matchmaking of owners of goods with freight transportation providers
- New business model: *virtual logistics platforms*



# MAS FOR FREIGHT BROKERING





# FREIGHT BROKER AGENT

- Declarative optimization model of the *FBAgent*:
  - Defined as type of Vehicle Routing with Pickup and Delivery Problem – VR-PDP
  - Computing optimal schedules using Constraint Logic Programming – CLP.



# VR-PDP

- Well-known problem in operation research:

Given:

- A set of customers
- A vehicle pool to service deliveries

Determine:

- A minimum cost set of vehicle routes that *services* all customers

- Service:

- Pickup = freight loading point
- Delivery = freight unload point

# PROBLEM

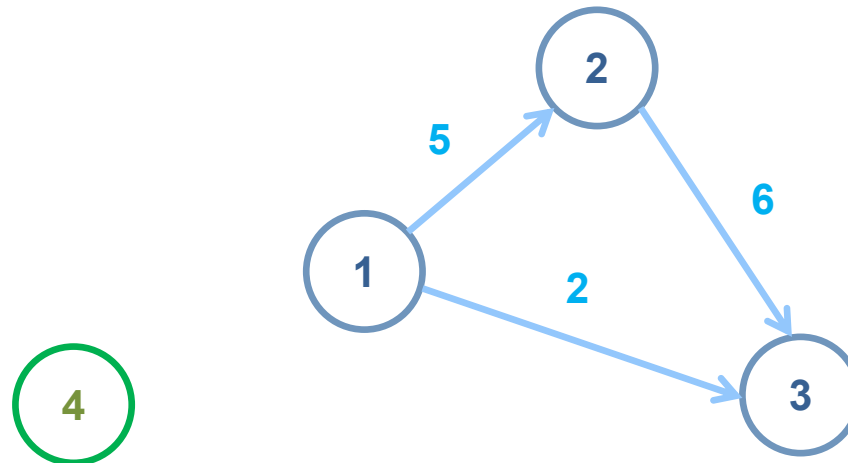
Tuple  $\langle \mathcal{L}, \mathcal{O}, \mathcal{T}, \Delta \rangle$  s.t.:

1.  $\mathcal{L} =$  **locations of interest**  $= \mathcal{P} \cup \mathcal{H}$ 
  - $\mathcal{P} = \{1, 2, \dots, k\} =$  **pickup and delivery points**,  $k > 0$
  - $\mathcal{H} = \{k + 1, \dots, k + h\} =$  **truck home locations**,  $h \geq 0$
2.  $\mathcal{O} =$  **customer orders**,  $|\mathcal{O}| = n$ .  $O_i = (OS_i, OD_i, C_i)$  s.t. :
  - $OS_i, OD_i \in \mathcal{P}$ ,  $OS_i \neq OD_i$  are pickup and delivery points
  - $C_i > 0 =$  requested capacity of order  $i$ . Obs:  $2 \leq k \leq 2n$ .
3.  $\mathcal{T} =$  **set of trucks**,  $|\mathcal{T}| = t$ ,  $T_i = (H_i, \Gamma_i)$  s.t.
  - $H_i \in \mathcal{H}$ ,  $\Gamma_i > 0$  are **home & provided capacity** of truck  $i$ .
4.  $\Delta = (k + h) \times (k + h)$  real matrix s.t.  $\Delta_{ij} > 0$  are **distances** between  $1 \leq i \neq j \leq k + h$ .



# EXAMPLE PROBLEM

- $k = 3$  pickup and delivery points
- $n = 3$  orders:  $\mathcal{O} = \{(1 \rightarrow 2, 5), (1 \rightarrow 3, 2), (2 \rightarrow 3, 6)\}$
- $t = 2$  trucks:  $\mathcal{T} = \{(4, 7), (4, 5)\}$ . Trucks home is 4, so there are  $h = 1$  home locations



# SCHEDULE

Tuple  $\langle X, M, S, D \rangle$  s.t.:

1.  $X \in \{1, 2, \dots, k\}^m =$  **hops sequence** of truck routes. Each location is visited, each order needs two hops,  $k \leq m \leq 2n$ .
2.  $M \in \{0, 1, \dots, m\}^t$  s.t.  $M_l$  is the **number of hops of each truck**  $l$ . Total number of hops:  $m = \sum_{l=1}^t M_l$ .
  - $M_l \geq 0$  allows solutions of “*at most*”  $t$  trucks.
  - $M_l \geq 1$  constraints solutions to use “*exactly*”  $t$  trucks.
3.  $S, D \in \{0, 1\}^{m \times n}$  are Boolean matrices s.t.:
  - $S_{ij} = 1$  iff  $X_i$  is **pickup point** of order  $j$ , else  $S_{ij} = 0$ .
  - $D_{ij} = 1$  iff  $X_i$  is **delivery point** of order  $j$ , else  $D_{ij} = 0$ .

# EXAMPLE SCHEDULE

- $k = 3$  pickup and delivery points
- $n = 3$  orders:  $\mathcal{O} = \{(1 \rightarrow 2,5), (1 \rightarrow 3,2), (2 \rightarrow 3,6)\}$
- $t = 2$  trucks:  $\mathcal{T} = \{(4,7), (4,5)\}$ . Trucks home is 4, so there are  $h = 1$  home locations

Truck $t$	1			2	
$\Gamma$	Maximum capacity 7			Maximum capacity 5	
$T$	Capacity 5	Capacity 6	Capacity 0	Capacity 2	Capacity 0
$S, D$	Load 1: 1,5	Unload 1: 2,5 Load 3: 2,6	Unload 3: 3,6	Load 2: 1,2	Unload 2: 3,2
$X$	1	2	3	1	3
Hop $i$	1	2	3	4	5

# STATE SPACE SIZE

- $|X| = m, X_i \in \{1, 2, \dots, k\}, k \leq m \leq 2n$
- $|S| = 2^{mn}, |D| = 2^{mn}$
- $Size = \sum_{m=k}^{2n} 2^{mn} 2^{mn} m^k$
- $n = 5, k = 6$
- $Size = 2^{60}6^6 + 2^{70}7^6 + 2^{80}8^6 + 2^{90}9^6 + 2^{100}10^6 > 10^{36} !!$

# CONSTRAINTS

- Pickup & Delivery Definition
- Non-Redundant Hops
- Pickup Precedes Delivery
- Service Completeness
- Truck Assignments
- Capacity Constraints
- Optimization Cost

# PICKUP PRECEDES DELIVERY

- For all hops  $i, k$  if there exists an order  $j$  such that  $i$  is the pickup point of  $j$  and  $k$  is the delivery point of  $j$  then  $i$  precedes  $k$ , so:

$$(\forall i, k) ((\exists j)((S_{ij} = 1) \wedge (D_{ij} = 1)) \Rightarrow (i < k))$$

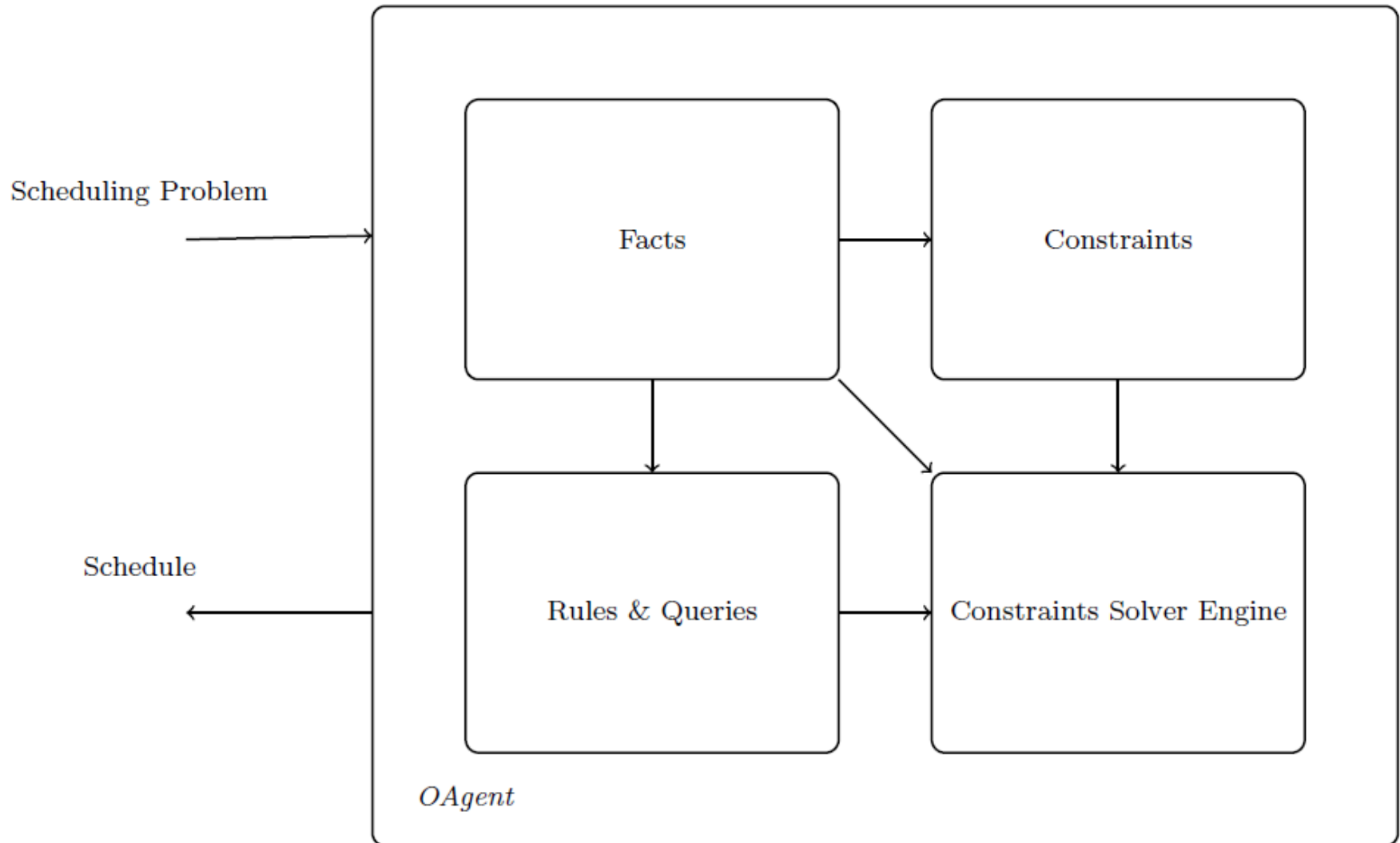
- Using  $p \Rightarrow q \equiv \neg q \Rightarrow \neg p$  we obtain a simpler form:

$$(\forall i, j, k)((i \geq k) \Rightarrow ((S_{ij} = 0) \vee (D_{ij} = 0)))$$

# CONSTRAINT LOGIC PROGRAMMING

- **CLP program** = facts and rules built using predicates:
  - i. Normal Prolog predicates handled by Prolog engine
  - ii. Constraints handles by special constraint solvers
  
- **CLP program structure**:
  - i. Definition of variables and domains
  - ii. Definition of constraints
  - iii. Definition of cost variable
  - iv. Search for optimal solution

# OPTIMIZATION AGENT – *OAGENT*





# SCHEDULING PROBLEM AS PROLOG FACTS

```
number_of_orders(3).
number_of_cities(3).
number_of_trucks(3).
number_of_homes(1).
% order(OrderIdx, LoadIdx, UnloadIdx, Capacity)
order(1,1,2,5).
order(2,1,3,2).
order(3,2,3,6).
% truck(TruckIdx, HomeIdx, MaxCapacity)
truck(1,4,7).
truck(2,4,4).
truck(3,4,5).
% distance(LocationI, LocationJ, DistanceIJ)
distance(1,2,10).
distance(2,1,10).
% ...
distance(4,3,10).
```

# SOLUTION PREDICATE

```
solution(_m,_n,_t,M,S,D,X,Ds) :-  
    domains_and_variables(_m,_n,_t,M,S,D,X,Delta) ,  
    constraints(_m,_n,_t,M,S,D,X) ,  
    search_query(X,S,D) ,  
    compute_distances(_m,_t,M,Delta,X,Ds) .
```

# IMPLEMENTATION OF CONSTRAINTS

- Logic:

$$(\forall i, j, k)((i \geq k) \Rightarrow ((S_{ij} = 0) \vee (D_{ij} = 0)))$$

- ECLiPSe-CLP:

```
constraint_2(M,N,S,D) :-
    ( for(J,1,N), param(M,S,D) do
        ( for(I,1,M), param(J,S,D) do
            ( for(K,1,I), param(I,J,S,D) do
                S[I,J] #= 0 or D[K,J] #= 0
            )
        )
    )
).
```

# SEARCH PROCESS

- Top level search

- Instantiates number of hops  $m$  and vector  $M$  of route lengths of each truck such that:

$$\sum_{l=1}^t M_l = m$$

- Main search

- Searches for problem solutions  $X, S, D$  for fixed values of  $m$  and  $M$ .

# SEARCH QUERY

Stochastic  
search

```

search_query (X, S, D) :-
    search ([ ] (X, S, D), 0,
            most_constrained,
            indomain_random,
            lds (2),
            [nodes (28000)]
    ).
    
```

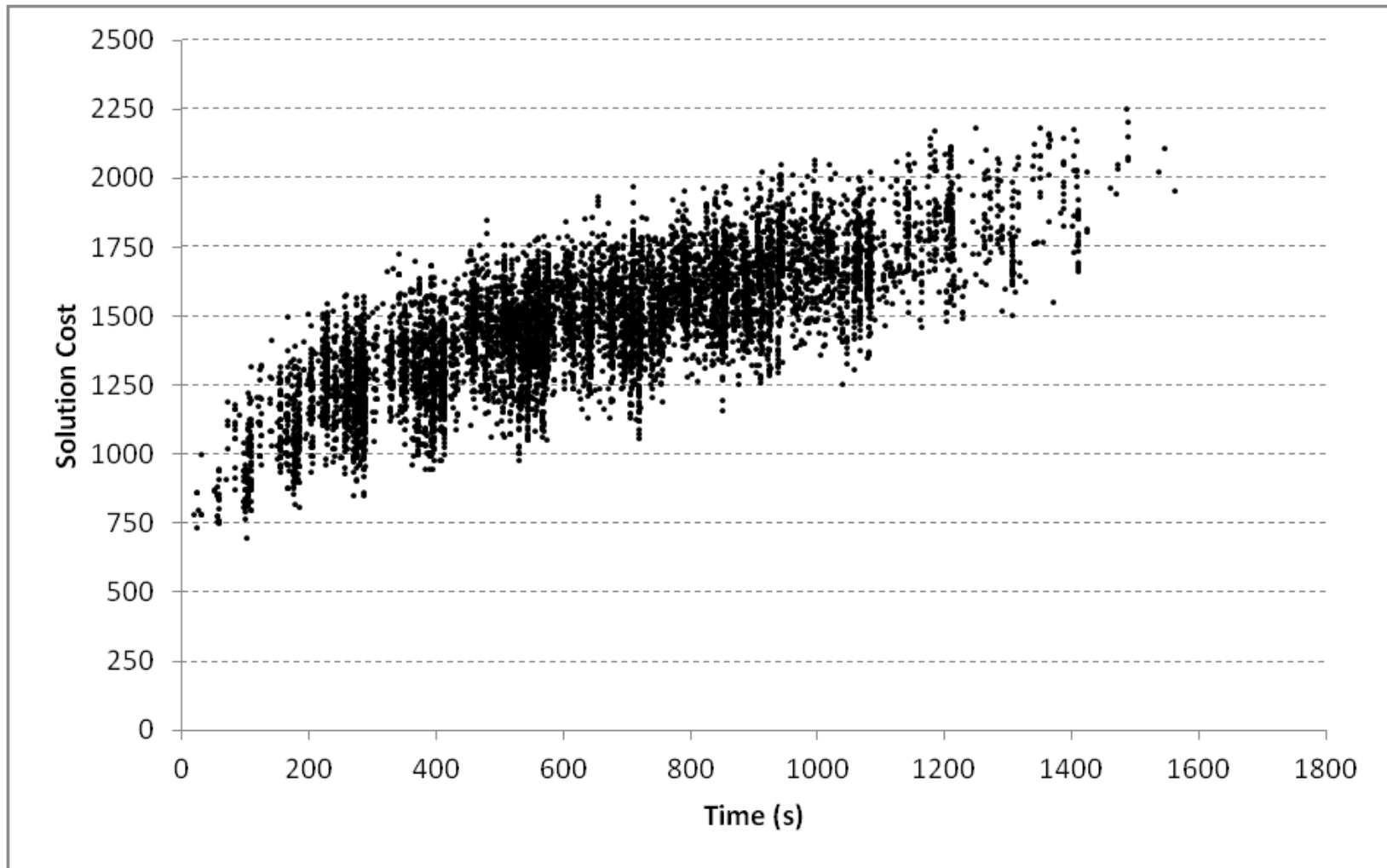
Limited  
discrepancy  
search

# DATA SET & SEARCH CONFIGURATION

Data set	$n$	$t$	$k$	Top search	Main search	Timeout/run [s]	# Runs	# nodes/ main search	Limit reached?
10-4	10	4	6	Complete	lds(1)	60	20	10,000	No
10-8	10	8	6	lds(3)	lds(1)	90	20	10,000	No
10-12	10	12	6	lds(3)	lds(2)	150	20	12,000	Yes
15-4	15	4	6	lds(3)	lds(1)	90	20	10,000	No
15-8	15	8	6	lds(3)	lds(1)	150	20	10,000	No
15-12	15	12	6	lds(3)	lds(2)	210	20	14,000	Yes
20-4	20	4	6	lds(3)	lds(1)	120	20	12,000	Yes
20-8	20	8	6	lds(2)	lds(2)	180	20	18,000	Yes
20-12	20	12	6	lds(2)	lds(2)	240	20	16,000	Yes
25-4	25	4	6	lds(2)	lds(2)	150	20	12,000	Yes
25-8	25	8	6	lds(2)	lds(2)	210	20	12,000	Yes
40-4	40	4	6	lds(3)	lds(2)	300	12	38,000	Yes

$n$  is the number of orders,  $t$  is the number of trucks, and  $k$  is the number of locations

# SOLUTIONS OF 10-4 PROBLEM



# REFERENCES

1. Amelia Bădică, Costin Bădică, Florin Leon, Ionuț Buligiu: *Modeling and Enactment of Business Agents Using Jason*, In: Proc. 9<sup>th</sup> Hellenic Conference on Artificial Intelligence, SETN '16, ACM, (2016) doi: 10.1145/2903220.2903253
2. Costin Bădică, Alex Becheru and Samuel Felton. *Integration of Jason Reinforcement Learning Agents into an Interactive Application*. In: Proc. 19th International Symposium on Symbolic and Numeric Algorithms for Scientific Computing, (SYNASC 2017), 361-368, IEEE, (2017) doi: 10.1109/SYNASC.2017.00065
3. Costin Bădică, Florin Leon, Amelia Bădică. *Freight transportation broker agent based on constraint logic programming*. Evolving Systems. Springer (2018) doi: 10.1007/s12530-018-9230-3



